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**EXAM ID NUMBER: \_\_\_\_\_**

**COURSE NUMBER: AMCS 241**

**PROBLEM: 1**

## Problem 1 (20 Points)

### Part 1 (10 points)

1) (7 points) Let  $X$  be a continuous random variable. Find a general formula for the probability density function (PDF) of  $Y=|X|$ .

2) (3 points) Evaluate your formula if  $X$  is a standard normal random variable.

Hint: The PDF of a normal random variable with mean  $\mu$  and standard deviation  $\sigma$  is given by

$$f_X(x) = \frac{1}{\sqrt{2\pi} \sigma} \exp\left(-\frac{(x - \mu)^2}{2\sigma^2}\right).$$

### Part 2 (10 points)

A random process  $X[n]$  for  $-\infty < n < \infty$  consists of independent random variables with

$$X[n] \sim \begin{cases} \text{Gaussian with zero mean and unit variance for } n \text{ even i.e. } \mathcal{N}(0, 1) & \text{for } n \text{ even} \\ \text{Uniformly distributed over } [-\sqrt{3}, \sqrt{3}] & \text{for } n \text{ odd i.e. } \mathcal{U}(-\sqrt{3}, \sqrt{3}) \end{cases}$$

1) (5 points) Is the random process  $X[n]$  wide sense stationary (WSS)?

2) (5 points) Is  $X[n]$  stationary?

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**COURSE NUMBER: ACMS 241**

**PROBLEM: 2**

## Problem 2 (20 Points)

### Part 1 (10 points)

Let  $X$  and  $Y$  be two discrete random variables with joint probability mass function (PMF) given by

$$p_{X,Y}[i, j] = p_1 p_2 (1 - p_1)^i (1 - p_2)^j \quad i = 0, 1, \dots; j = 0, 1, \dots$$

where  $0 < p_1 < 1$ ,  $0 < p_2 < 1$ . Find  $P[Y > X]$ .

### Part 2 (10 points)

1) (8 points) If the discrete white Gaussian random process  $X[n]$  with  $\sigma_x^2=1$  is input to a differencer to generate the output random process  $Y[n]=X[n]-X[n-1]$ , find the joint probability density function (PDF) of the samples  $Y[0]$ ,  $Y[1]$ .

2) (2 points) Are the samples  $Y[0]$  and  $Y[1]$  independent?